

AN EMPIRICAL
ANALYSIS OF THE
PESETA'S EXCHANGE
RATE DYNAMICS

Juan Ayuso and Juan L. Vega

AN EMPIRICAL ANALYSIS OF THE PESETA'S EXCHANGE RATE DYNAMICS (*)

Juan Ayuso and Juan L. Vega

(*) Prepared for the meeting of central bank econometricians and model builders held at the BIS on 14th and 15th December 1995. We are grateful to W. Melick for his excellent discussion and to the participants at the meeting. We also thank O. Bover and J. J. Dolado for helpful comments.

Banco de España - Servicio de Estudios
Documento de Trabajo nº 9613

In publishing this series the Banco de España seeks to disseminate studies of interest that will help acquaint readers better with the Spanish economy.

The analyses, opinions and findings of these papers represent the views of their authors; they are not necessarily those of the Banco de España.

ISSN: 0213-2710

ISBN: 84-7793-477-0

Depósito legal: M-16546-1996

Imprenta del Banco de España

ABSTRACT

The paper addresses the issue of the role of exchange rate jumps. The short-run dynamics of the peseta's effective exchange rate vis-à-vis OECD countries over the period 1974:1-1995:9 is estimated using a PPP-based error-correction model enlarged with additional terms allowing for the possibility of unusual jumps. The estimates point to an exchange rate characterized by a slow adjustment towards the long-run equilibrium determined by relative prices in the tradable sector, while jumps accelerate this adjustment process. Probit models relating the probability of such jumps to some macroeconomic fundamentals are also estimated.

1. Introduction

In the early 80's Meese and Rogoff (1983) puzzled most economists by showing that despite the existence of several competing theories to explain free floating exchange rate movements¹, none were able reliably to improve the forecasts from a simple random walk model. More than ten years later their results remain in place. In a recent survey, Frankel and Rose (1994) conclude that standard theoretical models still fail to predict future free floating exchange rate changes in the short and medium term.

Empirical results are also disappointing regarding our ability to explain future exchange rate movements for currencies that belong to ~~managed~~ exchange rate regimes like the Exchange Rate Mechanism (ERM) of the European Monetary System (see Garber and Svensson, 1994), in spite of the convincing theoretical work pioneered by Krugman (1991).

The recent periods of turbulence in the foreign exchange markets have renewed interest in the difficult task of identifying the driving forces of exchange rate movements in the short and medium term. In this paper we estimate a model explaining the dynamics of the effective exchange rate of the peseta vis-à-vis OECD countries². Our model takes into account that this exchange rate is neither under the direct control of the monetary authorities (as it includes bilateral exchange rates against currencies that are, or have been, outside the ERM) nor completely flexible (because it includes bilateral ~~managed~~ exchange rates). It also pays special attention to the role of the jumps in the exchange rate that we observe from time to time.

The empirical model relies, on the one hand, on the results in Pérez-Jurado and Vega (1994), who showed that purchasing power parity

¹ Surveys on this topic are legion. See, for example, MacDonald and Taylor (1989).

² See Bajo and Sosvilla (1993) for a survey on the empirical evidence on different theoretical models to explain the peseta's exchange rate dynamics.

(PPP) holds in the long run when tradable-good prices are considered. On the other hand, the model builds on the work by Ayuso and Pérez-Jurado (1995) where unusual jumps in the exchange rates of ERM currencies are explained in terms of real exchange rate deviations from a reference value and different variables that determine the costs for the monetary authorities of maintaining a given exchange rate.

In particular, the starting point of the analysis is an error correction model (ECM) for the first difference of the peseta's (log) effective/exchange rate. This model is enlarged with additional terms which take into account the possibility of a jump in the exchange rate. Following Ayuso and Pérez-Jurado (1995) the size of the jumps are assumed to be a function of PPP deviations. The probability of the jumps is also estimated under Probit models that allow us to investigate to what extent macroeconomic variables may help predict such jumps.

According to the estimate of our modified ECM equation, exchange rate jumps act as accelerators of the speed of adjustment to the long run equilibrium. On the other hand, although a number of macroeconomic variables can help explain why exchange rates jump, their predictive power is rather low.

The structure of the paper is the following. After this introduction, section 2 depicts the basic model. Section 3 deals with the estimate of the modified ECM equation and Section 4 is devoted to estimating the jump probabilities. Finally, Section 5 summarises the main results in the paper.

2.- Econometric framework

Our starting point is the work by Ayuso and Pérez-Jurado (1995). This paper addresses the issue of the decomposition of the expected devaluation rate into the likelihood of a devaluation and its expected size and puts forward, in the context of the ERM, the following univariate model for the bilateral peseta-Deutschemark exchange rate:

$$s_t = k + \Gamma(L) s_{t-1} + d_t + \epsilon_t$$

$$d_t = \begin{cases} d_t^* & \text{with prob. } Pr_{t-1} \\ 0 & \text{with prob. } 1 - Pr_{t-1} \end{cases} \quad (1)$$

where s_t is (the log of) the exchange rate; $\Gamma(L)$ is a general lag polynomial; d_t^* is the size of the exchange rate jump in the event of a devaluation; and Pr_{t-1} is the likelihood, at time $t-1$, of a devaluation occurring at time t .

It is also assumed that d_t^* depends on the vector of variables x_{t-1}^d and that a devaluation takes place when a given indicator c_t^* takes positive values. This indicator can be interpreted as the cost perceived by the government of maintaining the current parity. This cost depends on a vector of fundamentals x_{t-1}^c . Therefore:

$$d_t^* = \beta^d x_{t-1}^d + u_t^d \quad (2)$$

$$c_t^* = \beta^c x_{t-1}^c + u_t^c \quad (3)$$

$$Pr_{t-1} = \text{prob. } (u_t^c > -\beta^c x_{t-1}^c) \quad (4)$$

According to the results in Ayuso and Pérez-Jurado (1995), d_t^* depends exclusively on the deviations of the real exchange rate from a reference level, so that equation (2) can be rewritten as:

$$d_t^* = \beta_0 - \beta(tc r_{t-1} - tc r^*) + u_t^d = \lambda - \beta tc r_{t-1} + u_t^d \quad (2')$$

Neither c_t^* nor d_t^* are observable. The only information available to the econometrician is whether or not a devaluation has occurred and, conditional on its occurrence -and on an estimate of k and $\Gamma(L)$ -, its size (d_t^*). However, by defining a binomial variable:

$$\omega_t = \begin{cases} 1 & , \text{ if } c_t^* > 0 \\ 0 & , \text{ if } c_t^* \leq 0 \end{cases} \quad (5)$$

the parameters β^c can be estimated from a Probit model for ω_t . Given the Probit estimates, β^d can also be obtained including in equation (2) the well-known Heckman lambda. Nevertheless, Ayuso and Pérez-Jurado (1995) confined their attention to the direct estimation of β^d from a non-linear transformation of equation (2) which exploits the uncovered interest rate parity assumption and the information contained in the interest rate differentials.

In this paper the aforementioned framework is extended in a number of directions. First, a more general process for the exchange rate is allowed for by using the results in Pérez-Jurado and Vega (1994). In a multivariate-multicountry framework based on the Johansen procedure, Pérez-Jurado and Vega (1994) showed evidence that in the long run prices in the tradable sector (as proxied by the industrial price index) in Spain, Italy, France, U.K, Germany and USA, expressed in the same currency, tend to converge. This convergence implies that the bilateral and multilateral real exchange rates follow processes that tend towards a constant long-run equilibrium. Hence PPP holds in the long run when prices of non-tradable goods are excluded from the analysis.

This cointegration property allows us to extend equation (1) for the exchange rate by estimating the following ECM:

$$\Delta s_t = \mu - \delta(\Delta p - \Delta p^*)_{t-1} - \alpha \pi r_{t-1} + \sum_{i=1}^p \alpha_i \Delta s_{t-i} + \sum_{i=1}^p \beta_i \Delta^2 p_{t-i} + \sum_{i=0}^p \delta_i \Delta^2 p_{t-i}^* + u_t \quad (6)$$

where s_t , p_t and p_t^* , respectively, stand for (all variables in logs) the nominal exchange rate index vis-à-vis OECD countries (foreign currency/pesetas), the domestic industrial price index, and a weighted index of industrial prices in OECD countries; and $\pi r_t \equiv s_t + p_t - p_t^*$ is

the real exchange rate. The following statistical properties of the data are implicit in the specification of equation (6)³:

$$\begin{aligned} p_t &\sim I(2) & , & & p_t^* &\sim I(2) \\ s_t &\sim I(1) & , & & (p_t - p_t^*) &\sim I(1) \\ \Delta(p - p^*)_t &\sim I(0) & , & & \Delta cr_t \equiv s_t + p_t - p_t^* &\sim I(0) \end{aligned}$$

The second extension is related to the concept of exchange rate jumps. Ayuso and Pérez-Jurado (1995) confined their analysis to official devaluations of the peseta -i.e. realignments- during the ERM period (1989:6 onwards). In this paper the analysis is extended by considering as well cases where, although no devaluations occur, there are abrupt changes (both positive and negative) in the exchange rate. Such episodes will be labelled as jumps.

This extended concept has some advantages as it increases the number of observations on jumps, it allows us to include both depreciation and appreciation episodes and it is readily extended to the free-floating period. But it also presents some shortcomings. On the one hand, variable c_t^* must be reinterpreted as the short-term economic costs that agents, both public and private, perceive from maintaining a given level of nominal exchange rate. On the other hand, a problem of econometric identification arises as variable ω_t is no longer observable. In this latter respect the adoption of a fairly empirical approach is suggested by assuming that the exchange rate jumps whenever the absolute value of the residuals in equation (6) exceed some arbitrary critical value (θ).

In accordance with the extended concept of a jump, two variables (Q_t and D_t) are defined:

$$Q_t = \begin{cases} 0, & \text{if } \hat{u}_t < \theta \\ 1, & \text{if } \hat{u}_t \geq \theta \end{cases}$$

³ See Pérez-Jurado and Vega (1994) for a detailed description of unit root tests results.

$$D_t = \begin{cases} 0, & \text{if } \hat{u}_t > -\theta \\ 1, & \text{if } \hat{u}_t \leq -\theta \end{cases}$$

The first variable (Q_t) captures positive jumps, i.e. unusual appreciations of the exchange rate, while the second (D_t) captures negative jumps, i.e. unusual depreciations. These variables will enable, on the one hand, the estimation in section 4 of two Probit models relating the likelihood of jumps, both positive and negative, to economic fundamentals. On the other hand, they will also enable the estimation of the parameters in equation (2') explaining the size of the jumps⁴.

Residuals from equation (6) can be decomposed into two components: one capturing abrupt changes in the exchange rate (d_t), and the other a homoscedastic innovation (v_t):

$$u_t = d_t + v_t$$

Noting further that $d_t = (D_t + Q_t) d_t^*$ and substituting equation (2') into equation (6) yields:

$$\Delta s_t = \Phi' Z_{t-1} - \alpha \text{tcr}_{t-1} + \lambda (D_t + Q_t) - \beta (D_t + Q_t) \text{tcr}_{t-1} + \eta_t \quad (6')$$

$$\eta_t = (D_t + Q_t) u_t^d + v_t$$

where the vector Z_{t-1} groups all variables in (6) other than tcr_{t-1} and the residuals η_t are no longer homoscedastic. Instead:

$$E(\eta_t^2) = \begin{cases} \sigma_\eta^2 & \text{if } (D_t + Q_t) = 1 \\ \sigma_v^2 & \text{if } (D_t + Q_t) = 0 \end{cases}$$

⁴ In Vlaar (1994), jump probabilities and jump effects on the exchange rate dynamics are jointly estimated inside the ERM. Nevertheless, he has to assume that jump sizes are constant.

In the next section we estimate the exchange rate equation by GLS⁵ using monthly data over the sample 1974:7-1995:9. In order to test for asymmetries in the effects of positive and negative exchange rate jumps, we estimate a slightly different version of equation (6'):

$$\Delta s_t = \Phi' Z_{t-1} - \alpha tcr_{t-1} + \lambda^- D_t + \lambda^+ Q_t - \beta^- D_t tcr_{t-1} - \beta^+ Q_t tcr_{t-1} + \xi_t \quad (6'')$$

where:

$$E(\xi_t^2) = \begin{cases} \sigma_t^{2+} & \text{if } Q_t = 1 \\ \sigma_t^{2-} & \text{if } D_t = 1 \\ \sigma_v^2 & \text{otherwise} \end{cases}$$

3.- Exchange rate dynamics

As described in section 2, the proposed econometric strategy begins by estimating the error correction model for the changes in the (log) exchange rate given by equation (6). When this equation is estimated by OLS using monthly data spanning the period 1974:4-1995:9, the coefficient on the error correction term turns out to be $\hat{\alpha} = -.046$ (t-ratio = -2.3), consistent with the low speed of adjustment towards the PPP long-run equilibrium underlined in Pérez-Jurado and Vega (1994). More importantly, the estimated residuals (u_t) show, as expected from the discussion in the previous section, strong signs of heteroscedasticity and non-normality. Conversely, no signs of autocorrelation or ARCH are detected.

Chart 1 shows the scaled residuals from the estimation and **Table**

⁵ Observe that although (D_t+Q_t) , $(D_t+Q_t)tcr_{t-1}$, and η_t are different functions of \hat{u}_t , the chosen functional forms are such that both regressors are not correlated with the noise, thus making IV estimation unnecessary.

1 summarises some diagnostic tests on these residuals. The White (1980) HET test rejects unconditional homoscedasticity. The Doornik and Hansen (1994) N_2 statistic strongly rejects normality, indicating a distribution which is skewed to the left and has fatter tails than the normal distribution, i.e. extreme values are more common than in the normal distribution.

The latter observation provides some support to the proposed decomposition of the residuals into two components: the first (d_t) capturing abrupt changes in the exchange rate -jumps-, and the second (v_t) a homoscedastic innovation. The bottom part of Table 1 reports some statistics in this respect showing the number of jumps in the sample according to our various empirical definitions of jumps. Depending on θ , there are 20 ($\theta=2\%$), 25 ($\theta=1.75\%$) and 34 ($\theta=1.5\%$) jumps, representing, respectively, 7.8%, 9.8% and 13.4% of the sample.

The variables D_t and Q_t were defined as dummies which take values equal to one whenever there is a jump and zero otherwise. Again, depending on θ , we have three pairs (D_t , Q_t). Results for GLS estimates of the preferred specification of equation (6'') are summarized in Table 2. The bottom part of the table reports some diagnostic tests on the transformed residuals that are shown in Chart 2.

Some features are worth mentioning. Firstly, the point estimate of α , the parameter that measures the speed of adjustment towards the long-run equilibrium in the absence of jumps, is somewhat above 2% (with t-ratios ranging from 2.0 to 2.7), smaller than in the estimation of equation (6). The remaining point estimates are quite similar to those of equation (6).

Secondly, exchange rate jumps act as an accelerator mechanism towards restoring the long-run equilibrium defined by PPP. For negative jumps -i.e. unusual depreciations- the parameter β^- that measures this acceleration effect (how much of the accumulated gain or loss in competitiveness is reverted when there is a jump) is estimated between 13% and 19%, depending on the definition of jump, and close to that estimated in Ayuso and Pérez-Jurado (1995) when the most restrictive

definition is used ($\theta=2\%$). For positive jumps -i.e. unusual appreciations- this accelerator mechanism is weaker. The β^+ parameter ranges from 0, for the most restrictive definition of jump ($\theta=2\%$), to 6%, when θ equals 1.5%. In the intermediate case ($\theta=1.75\%$) λ^+ and β^+ t-ratios are well below 1, although the point estimates imply that the normal speed of the adjustment towards PPP equilibrium is doubled. In general terms, the precision of these estimates is low because of the lack of degrees of freedom. This leads to low t-ratios, although the effects clearly seem economically meaningful. Moreover, our λ^+ 's and β^+ 's estimates imply that the forecasted size of (ex-post) observed jumps⁶ is always correctly signed.

Finally, diagnostic tests performed on the transformed residuals reveal no signs of autocorrelation, ARCH, unconditional heteroscedasticity or misspecification as reported, respectively, by the LM [Harvey, 1990], ARCH [Engle, 1982], HET [White, 1980] and RESET [Ramsey, 1969] tests. Normality is not rejected at standard confidence levels, even in column 1 where only negative jumps are added to equation (6). The normality test statistic decreases⁷ from more than 300 to values around 5. Also, H^1 and H^2 [Hansen, 1992] tests show no signs of within-sample parameter instability.

Overall, results on the estimation of the exchange rate equation given by (6'') seem quite satisfactory, especially when θ is equal to 1.5%. The estimates point to an exchange rate characterised by a slow adjustment towards the long-run equilibrium determined by relative prices in the tradable sector. Occasionally, unusual abrupt changes occur, acting as an accelerator mechanism of this adjustment process. This accelerator effect is stronger when the jump implies an unusual depreciation.

Exchange rate jumps, both positive and negative, take place when

⁶ That is, $\lambda^- + \beta^- \text{tcr}_{t-1}$ if the jump is negative, or $\lambda^+ + \beta^+ \text{tcr}_{t-1}$ if it is positive.

⁷ It should be clear that our approach is a parsimonious modelling of jumps and does not involve the usual jump by jump intervention analysis.

economic agents perceive that maintaining a given level of nominal exchange rate is costly in the short run. Which macroeconomic fundamentals affect this perception is analysed in section 4.

4. Jump probabilities

In this section we analyse to what extent fundamental macroeconomic variables can help anticipate future jumps in the peseta's effective nominal exchange rate.

The probability that agents assign to a future jump in the exchange rate plays an important role in explaining the credibility of exchange rate commitments like the ERM. Nevertheless, the literature has paid more attention to credibility indicators that take into account not only such probability but also the expected size of the jump. Only a few papers have focused on estimating jump or realignment probabilities inside the ERM (see, for instance, Mizrach, 1993 and Gutiérrez, 1994) and they do not include the peseta's exchange rate. Recently, Ayuso and Pérez-Jurado (1995) estimate the probability of realignment of the bilateral exchange rate of the peseta (and other ERM currencies) against the Deutschemark and provide an empirical model that explains this probability in terms of the general performance of the ERM, a reputation effect, and the policy dilemma entailing the need for an interest rate level difficult to square with the position in the economic cycle. In any case, in all these papers jumps in exchange rates are associated with central parity realignments and always imply an unusual depreciation of the considered currency against the Deutschemark. In contrast with that approach, jumps in the peseta's effective exchange rate are more difficult to define.

As commented in sections 2 and 3, in this paper we follow an empirical approach to define exchange rate jumps and consider different critical sizes which allow for a reasonable number of jumps (between 8% and 14% of the sample size). Therefore, in our case, jumps are positive (i.e. an unusual appreciation) and negative (i.e. an unusual depreciation). Likewise, it is worth noting that jumps over the ERM period other than those associated with changes in central parities are included, as well as jumps over the non-ERM period that were not

preceded by any official announcement.

We fit the probabilities of both an unusual depreciation; and an unusual appreciation in the exchange rate over the next month by estimating two Probit models, one for positive jumps and the other for negative ones. This approach merits some comment.

Strictly speaking, the exchange rate can show a positive jump, a zero jump or a negative jump at any time. Thus, we face a multinomial qualitative variable taking three possible values. However, as can be seen in McFadden (1984), multinomial qualitative response models are rather rigid and restrictive, like the multinomial Logit model, or have high computational requirements, like the multinomial Probit model. Instead, our approach relies on binomial Probit models that are both flexible and easier to implement. Nevertheless, it does not guarantee that the adding up of negative and positive jump probabilities is below 1. Our results show, however, that this restriction has not been binding at any time in our sample.

Regarding the choice of the explanatory variables, we consider a relatively wide set of macroeconomic variables which, according to economic theory and to the results in the above-mentioned papers, could be arguments in the cost function described in section 2 and, therefore, help explain the probability of exchange rate jumps: real exchange rate, current-account deficit, inflation differential and variables capturing the relative position in the business cycle such as the unemployment rate, the output growth rate, the real interest rate or the capacity utilisation index. Naturally, these variables are conveniently lagged in order to avoid simultaneity problems.

The maximum likelihood parameter estimates of the Probit models are shown in Tables 3 and 4. Charts 3, 4 and 5 show the fitted probabilities. A number of results are worth commenting.

Parameter estimates in Table 3 exhibit correct signs although, in several cases, they are only marginally significant. According to these estimates, the better the cyclical position (the higher the capacity

utilisation is) the lower the probability of an unusual depreciation. The higher the accumulated real appreciation (over the last 12 months), the higher the negative jump probability, although this effect is less important after the entry of the peseta into the ERM. In the same vein, the higher the current-account deficit, the higher the probability of an unusual depreciation. This effect, however, disappears after the peseta's entry into the ERM⁸. Finally, the exchange rate regime change in June 1989 increased the probability of an unusual depreciation and opened the door to a new variable capturing the policy dilemma that entails the need for a domestic interest rate level in harmony with the new exchange rate commitment, but difficult to square with the cyclical position. The greater this dilemma, the greater the probability of an abrupt depreciation⁹.

If we focus on the analysis of the probability corresponding to months in which jumps have effectively occurred, the mean probability corresponding to these months is clearly higher than mean probability in the remaining months. Histograms (not-provided) show that probabilities are distributed quite differently in the months in which jumps are observed. This is also the case for positive jumps.

Point estimates in Table 4 show, however, some wrong signs. This is the case for the cyclical position and for the accumulated real appreciation, during the outside-the-ERM period, although the first one is not statistically significant and the second is only marginally significant. After June 1989, however, both variables are correctly signed and are significant: the probability of an unusual appreciation increases if the cyclical position improves or the real exchange rate has depreciated in the last 12 months. Contrary to Table 3, the entry of the peseta into the ERM reduced the probability of positive jumps. Again, the mean probabilities corresponding to months in which positive jumps have been observed are quite above those for the remaining months.

⁸ To be more precise, the parameter changes its sign and is not statistically significant.

⁹ Other variables have t-ratios below 1 and, sometimes, are wrong signed.

In Tables 3 and 4, results are very similar for jumps higher than 2%, 1.75% or 1.5%, although they are slightly better in the second case. Nevertheless, the pseudo- R^2 (see Estrella, 1995) range from 4% to 13% and are particularly poor for the positive jump models. The low predictive power of the Probit models is also confirmed by Charts 3, 4 and 5. These charts show that fitted probabilities are, in general, small¹⁰ and that there are relatively frequent peaks in periods in which the exchange rate has not jumped. Again, the picture is worse for positive than for negative jumps.

All in all, it can be said that according to our results, agents can hardly anticipate these unusual exchange rate jumps on the single basis of the macroeconomic fundamentals mentioned. This difficulty is especially clear when we look at the unusual appreciations. If agents were able to anticipate exchange rate jumps correctly, other factors such as expectations about political events or speculative bubbles should also play an important role. Unfortunately, these variables are difficult to measure and, therefore, difficult to include in a model like ours. Therefore, not too much can be said about the timing of the exchange rate jumps, though some information is provided as to what macroeconomic fundamentals may help reduce this uncertainty.

5. Conclusions

In this paper we investigate the dynamics of the peseta's effective exchange rate vis-à-vis OECD countries over the period from January 1974 to September 1995. The proposed empirical model enlarges upon results in Pérez-Jurado and Vega (1994) and Ayuso and Pérez-Jurado (1995). The former found that PPP holds in the long run when only prices in the tradable sector are considered. The latter estimated a model for the realignment probabilities inside the ERM and for the related jumps in the exchange rates. The results of both papers are embraced in the analysis

¹⁰ Over the ERM period, the estimated probability of an unusual depreciation is of the same order of magnitude as the realignment probability found in Ayuso and Pérez-Jurado (1995).

by estimating an equation for exchange rate dynamics that combines the features of an ECM and the possibility of unusual jumps. The size and the probability of these jumps are also estimated.

Jumps are defined in an empirical way and include not only 'official' devaluations as in Ayuso and Pérez-Jurado (1995) but also other abrupt depreciations or even appreciations that are above a given threshold. Several thresholds are considered with a view to testing for the robustness of the results.

The size of these unusual jumps depends on the deviation of the real exchange rate from its PPP value. Therefore, jumps enter the ECM playing the role of 'accelerators' in the path towards the long-run equilibrium. In particular, negative jumps, i.e. unusual depreciations, multiply the speed of the adjustment process by a factor ranging from 10 (for the most restrictive definition of jump) to 7 (for the least restrictive one). This accelerator effect is less clear for unusual appreciations. Only for the less restrictive definition of a jump is that effect significant, multiplying by 4 the speed of the adjustment.

Regarding the perceived probability of exchange rate jumps, two Probit models were estimated, one for each sort of jump. The results underscore that jump probabilities react to changes in certain fundamental macroeconomic variables: the current-account deficit (over the outside-the-ERM period), the accumulated real appreciation over the last twelve months and the position of the economy in the business cycle. Nevertheless, estimated probabilities are small and show relative peaks in periods in which exchange rate jumps have not occurred. Therefore there still seems to be an important degree of uncertainty in predicting the timing of jumps.

Appendix

All the calculations in the paper have been made using TSP 4.2B and PcGive 8.0. The following is a list of the test statistics reported in tables 1 and 2:

- $LM_{i,j}$ = the Lagrange Multiplier F-test for residual autocorrelation up to i^{th} order. See Harvey (1990) for a description.
- $ARCH_{1,j}$ = the Autoregressive Conditional Heteroscedasticity F-test reported in Engle (1982).
- $HET_{1,j}$ = the White (1980) F-test for heteroscedasticity. In this test, the null is unconditional homoscedasticity, and the alternative is that the variance of the residual depends on the levels and squared levels of the regressors.
- $RESET_{1,j}$ = the Regression Specification F-Test due to Ramsey (1969). This test may be interpreted as a test for functional form.
- Sk = skewness.
- Ek = excess kurtosis.
- N_2 = the Doornik and Hansen (1994) χ^2 -test for normality.
- H^1 = the Hansen (1992) within-sample parameter instability statistic for the residual variance σ^2 .
- H^2 = the Hansen (1992) joint statistic for within-sample stability of all the parameters in the model.

Table 1. SOME DIAGNOSTIC TESTS ON THE RESIDUALS FROM EQUATION (6)¹⁰

<u>OLS estimates. Sample: 1974/7-1995/9</u>			
	$LM_{12,216} = .892$	$ARCH_{7,216} = .058$	$HET_{41,186} = 1.545^*$
	$N_2 = 304.3^{**}$	$Sk = -3.738$	$Ek = 27.144$
	<u>Number of jumps (%)</u>		
	<u>Positive</u>	<u>Negative</u>	<u>Total</u>
$\theta = 2.0\%$	8 (4.7%)	12 (3.1%)	20 (7.8%)
$\theta = 1.75\%$	11 (5.5%)	14 (4.3%)	25 (9.8%)
$\theta = 1.5\%$	17 (6.7%)	17 (6.7%)	34 (13.4%)

¹⁰ See Appendix for a description of test statistics. * and ** stand for, respectively, rejection at 5% and 1% significance level.

Table 2. ESTIMATION OF (6'') AND SOME DIAGNOSTIC TESTS¹²

<u>Exchange Rate Equation: GLS estimates. Sample: 1974/7-1995/9</u>			
$\Delta s_t = \mu + \alpha_1 \Delta s_{t-1} + \alpha_2 (\Delta^2 s_{t-1} + \Delta^2 s_{t-2}) + \alpha_3 (\Delta^2 p_{t-1} + \Delta^2 p_{t-2})$ $+ \delta (\Delta p - \Delta p^*)_t + \alpha tcr_{t-1} + \lambda^- D_t + \beta^- D_t * tcr_{t-1} + \lambda^+ Q_t + \beta^+ Q_t * tcr_{t-1};$ $tcr_t \equiv s_t + p_t - p_t^*$			
	$\theta = 2\%$	$\theta = 1.75\%$	$\theta = 1.5\%$
μ	.1023 [2.09]	.0874 [1.97]	.1047 [2.68]
α_1	.1915 [4.37]	.2070 [5.36]	.2552 [6.71]
α_2	.0792 [3.35]	.0760 [3.48]	.0958 [4.81]
α_3	.1641 [2.22]	.1778 [2.62]	.2496 [4.19]
δ	-.2417 [2.07]	-.1958 [1.98]	-.2928 [3.29]
α	-.0225 [2.07]	-.0192 [1.96]	-.0232 [2.69]
λ^-	.8000 [1.42]	.6002 [1.40]	.5642 [1.53]
β^-	-.1879 [1.54]	-.1425 [1.48]	-.1331 [1.60]
λ^+	-	.1410 [0.66]	.2811 [1.77]
β^+	-	-.0265 [0.56]	-.0579 [1.65]
	$R^2 = .58$	$R^2 = .57$	$R^2 = .53$
	$LM_{12,234} = .63$	$LM_{12,234} = .51$	$LM_{12,232} = .53$
	$ARCH_{7,232} = .98$	$ARCH_{7,232} = .26$	$ARCH_{7,230} = 1.19$
	$HET_{16,228} = .36$	$HET_{16,228} = .46$	$HET_{18,225} = 1.01$
	$RESET_{1,245} = 1.12$	$RESET_{1,245} = 1.66$	$RESET_{1,243} = 3.02$
	$N_2 = 5.20$	$N_2 = 5.01$	$N_2 = 3.42$
	$H^1 = .09$	$H^1 = .15$	$H^1 = .12$
	$H^2 = 2.39$	$H^2 = 2.31$	$H^2 = 2.62$

¹² See Appendix for a description of test statistics. * and ** stand for rejection at 5% and 1%. T-ratios in brackets.

Table 3. PROBIT MODEL FOR THE PROBABILITY OF AN UNUSUAL EXCHANGE RATE DEPRECIATION

$Pr_{t-1}(D_t = 1) = \Phi(X_{t-1}^D \beta^D)$			
	Probability of a jump higher than		
	2%	1.75%	1.5%
Constant	6.74 [.93]	11.40 [1.62]	9.82 [1.51]
Cyclical Position ^(a)	-.13 [-1.38]	-.19 [-2.08]	-.15 [-1.85]
Accumulated Real Appreciation ^(b)	17.03 [2.12]	19.61 [2.41]	8.67 [2.15]
CA Deficit ^(c)	.05 [2.61]	.05 [3.05]	.02 [2.40]
ERM ^(d)	1.67 [2.08]	1.76 [2.19]	.46 [1.04]
Accum. Real App. times ERM	-16.39 [-1.87]	-16.17 [-1.85]	-8.60 [-1.40]
Policy Dilemma times ERM ^(e)	.07 [1.63]	.06 [1.44]	.06 [1.42]
pseudo-R ²	11%	13%	10%
RM ^(f)	5.16	5.08	3.53
RF ^(g)	4.5%	5.3%	6.5%

The model includes 246 observations corresponding to the period 75:2-95:7. t-ratios in brackets.

(a) Capacity Utilisation Index.

(b) Over the last 12 months.

(c) As a percentage of the GDP until 5:89, and 0 thereafter.

(d) Dummy variable that takes unit value as from 6:89.

(e) 1-month interest rate differential divided by 12-month output growth differential (proxied by industrial output growth).

(f) Ratio between mean probabilities in months with and without jumps.

(g) Relative frequency of the corresponding jumps in the sample.

Table 4. PROBIT MODEL FOR THE PROBABILITY OF AN UNUSUAL EXCHANGE RATE APPRECIATION

$Pr_{t-1}(Q_t = 1) = \Phi(X_{t-1}^Q \beta^Q)$			
	Probability of a jump higher than		
	2%	1.75%	1.5%
Constant	2.77 [.22]	7.88 [.80]	2.91 [.40]
Cyclical Position ^(a)	-.06 [-.39]	-.12 [-.99]	-.06 [-.61]
Accumulated Real Appreciation ^(b)	7.73 [1.83]	7.11 [2.04]	4.09 [1.63]
ERM ^(c)	-28.9 [-1.56]	-34.0 [-2.03]	-31.5 [-2.08]
Accum. Real App. times ERM	-30.1 [-2.78]	-29.5 [-2.79]	-25.6 [-2.59]
Cycl. Position times ERM	.38 [1.59]	.44 [2.04]	.40 [2.09]
pseudo-R ²	6%	5%	4%
RM ^(d)	4.95	2.65	1.94
RF ^(e)	3.3%	4.5%	6.9%

The model includes 246 observations corresponding to the period 75:2-95:7. t-ratios in brackets.

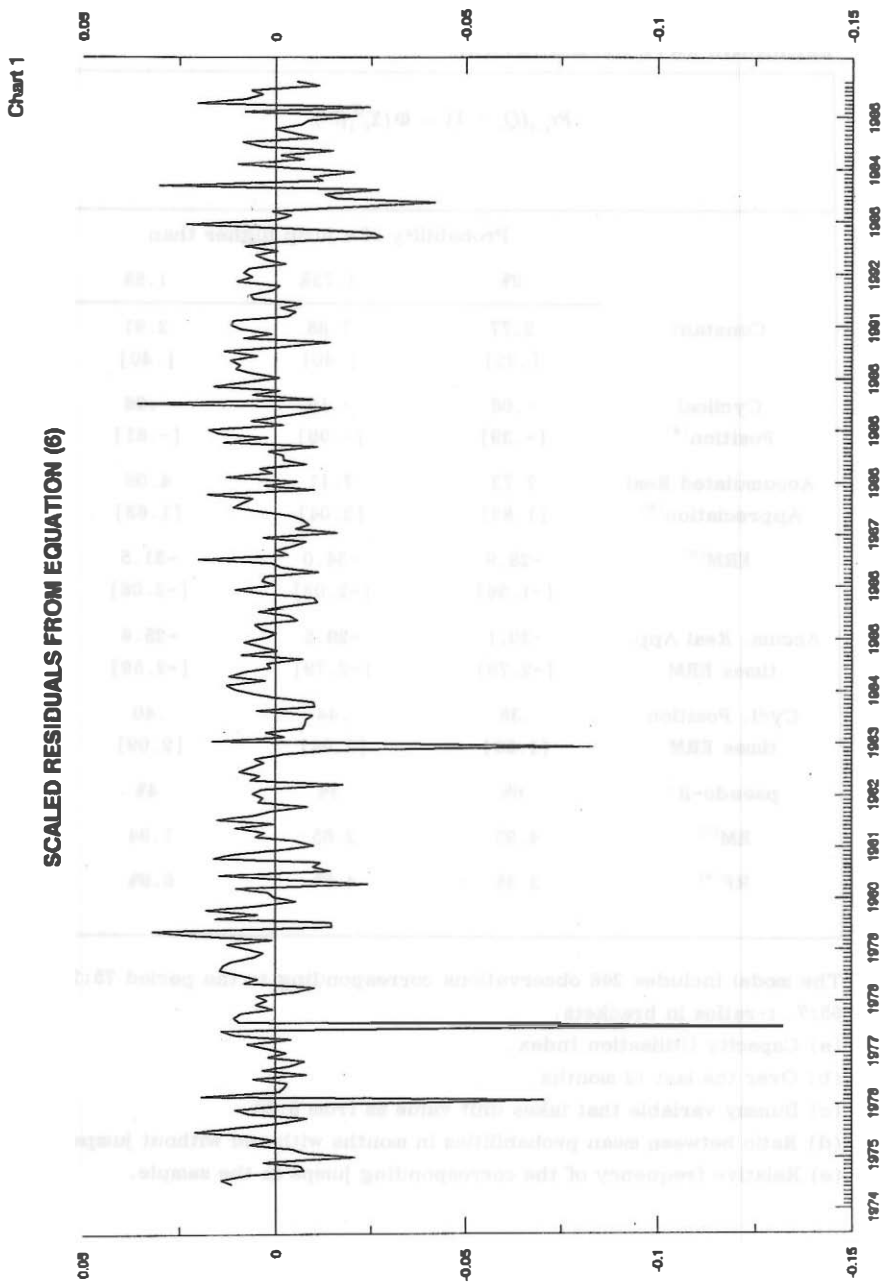
(a) Capacity Utilisation Index.

(b) Over the last 12 months.

(c) Dummy variable that takes unit value as from 6:89.

(d) Ratio between mean probabilities in months with and without jumps.

(e) Relative frequency of the corresponding jumps in the sample.



SCALED RESIDUALS FROM EQUATION (6')

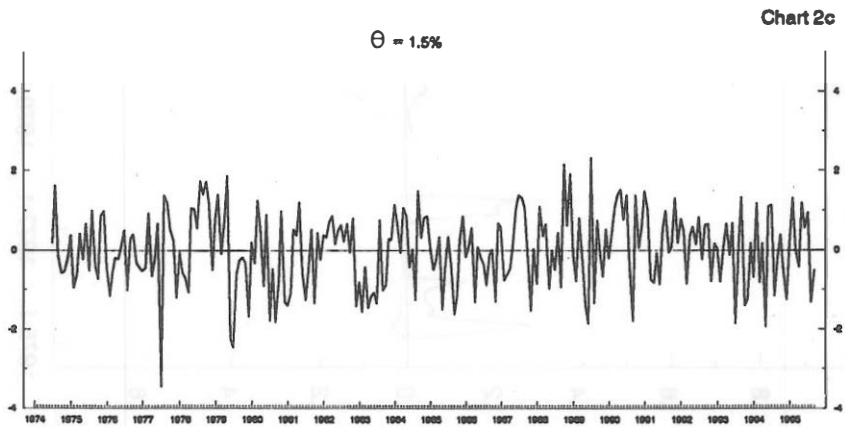
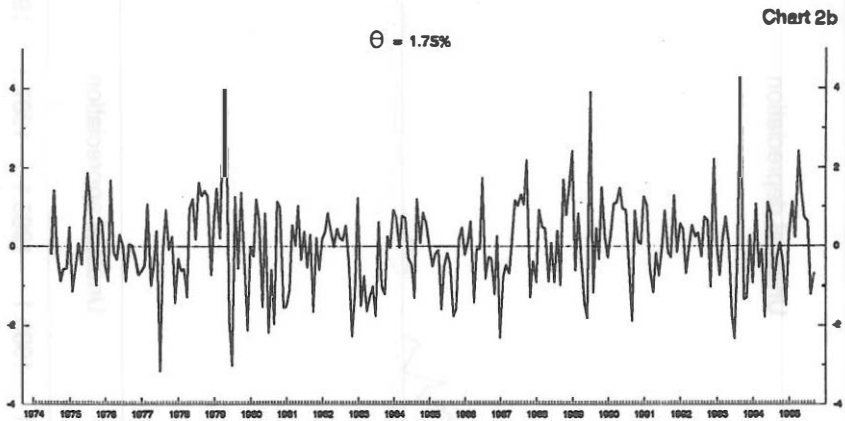
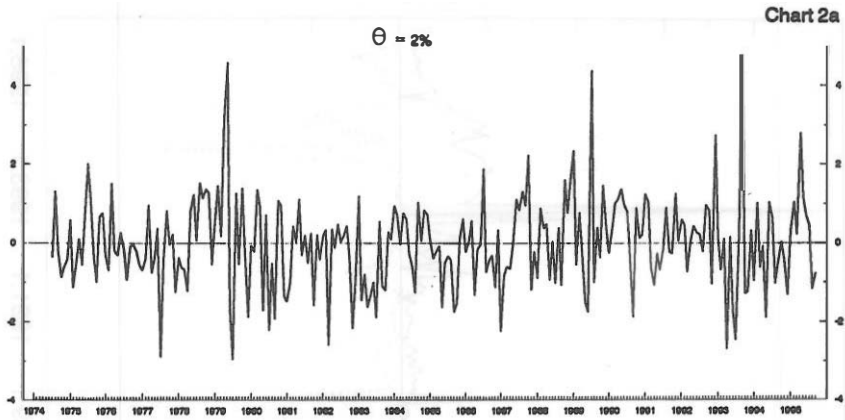
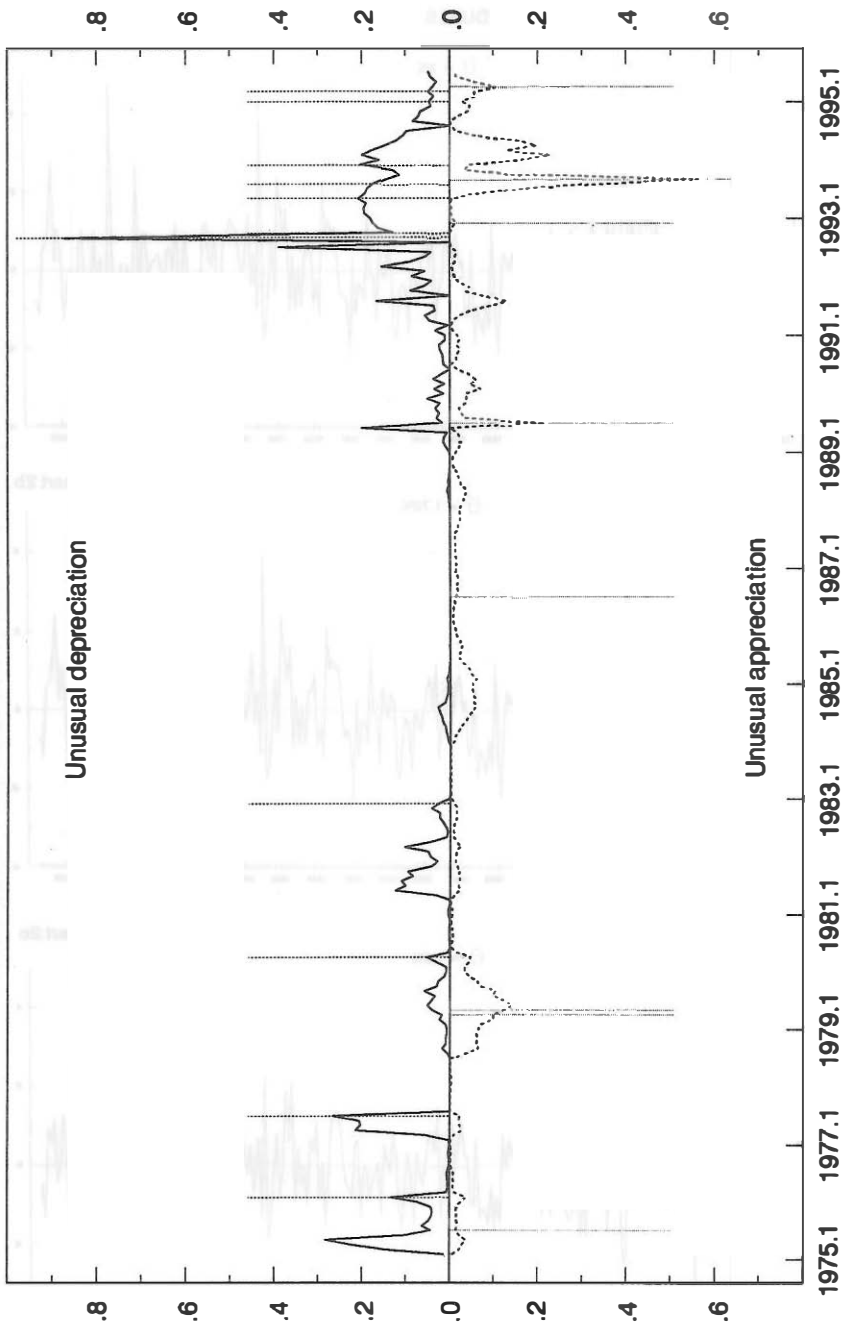


Chart 3

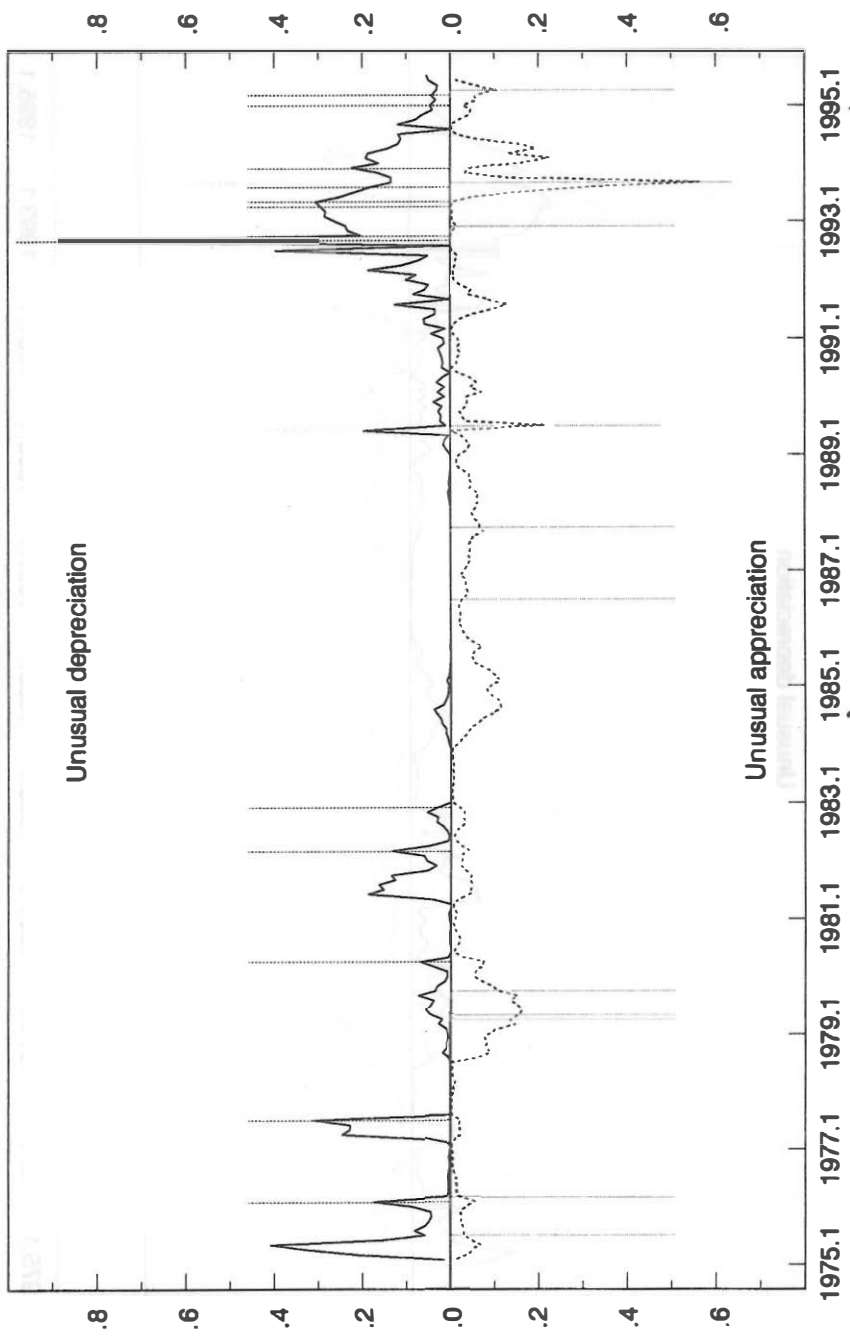
FITTED JUMP PROBABILITIES. JUMPS HIGHER THAN 2%



Note: Vertical lines correspond to observed jumps.

Chart 4

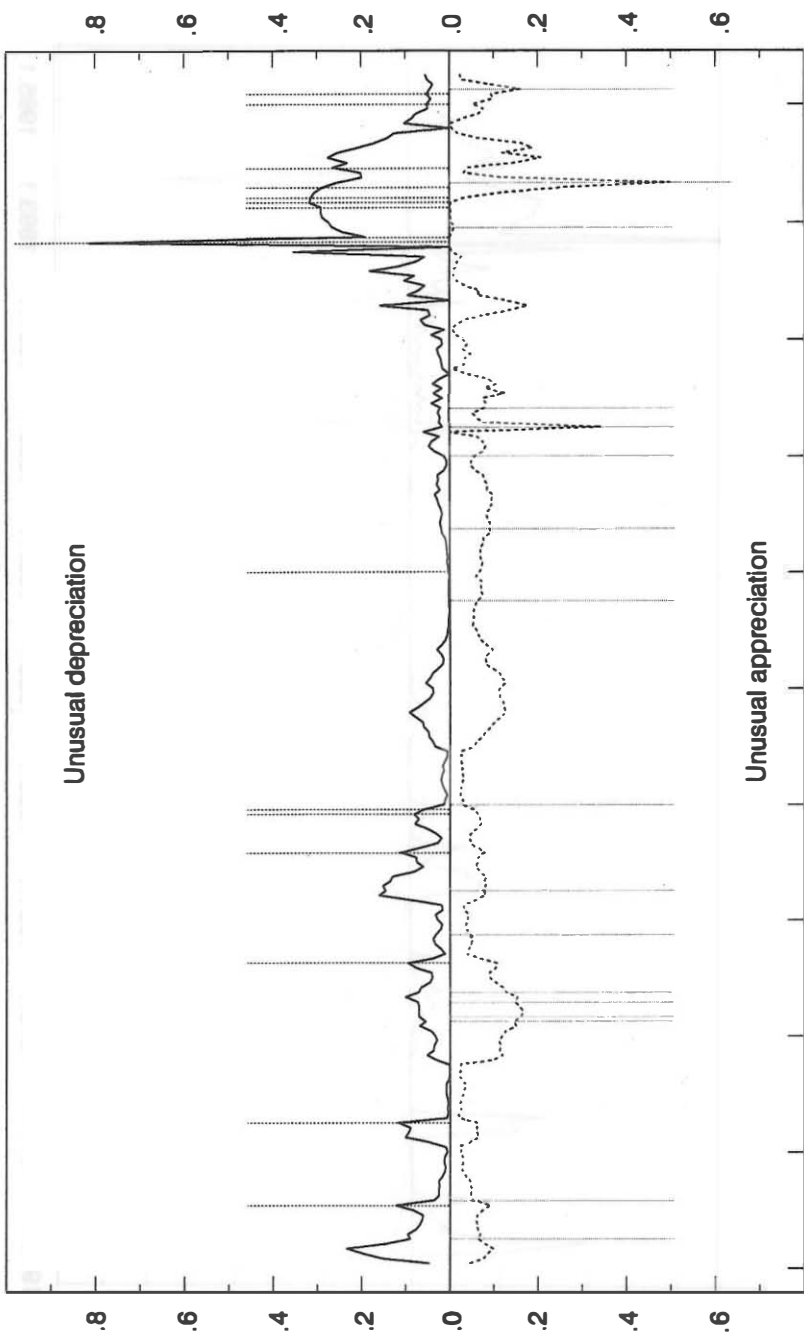
FITTED JUMP PROBABILITIES. JUMPS HIGHER THAN 1.75%



Note: Vertical lines correspond to observed jumps.

Chart 5

FITTED JUMP PROBABILITIES. JUMPS HIGHER THAN 1.5%



Note: Vertical lines correspond to observed jumps.

REFERENCES

- Ayuso, J. and M. Pérez-Jurado (1995), "Devaluations and Depreciation Expectations in the EMS", Banco de España Working Paper 9531.
- Bajo, O. and S. Sosvilla (1993), "Teorías del tipo de cambio: una panorámica", Revista de Economía Aplicada, No. 2, Vol. 1.
- Doornik J.A. and H. Hansen (1994), " A practical test of multivariate normality". Unpublished paper, Nuffield College.
- Engle, R.F. (1982), "Autoregressive conditional heteroscedasticity with estimates of the variance of United Kingdom inflation". Econometrica, 50.
- Estrella, A. (1995), "Measures of Fit with Dichotomous Dependent Variables: Critical Review and a New Proposal", Federal Reserve Bank of New York, Working Paper.
- Frankel, J.A. and A.K. Rose (1994), "A Survey on Empirical Research on Nominal Exchange Rates", NBER Working Paper No. 4865.
- Garber, P.M. and L.E.O. Svensson (1994), "The Operation and Collapse of Fixed Exchange Rate Regimes", Institute for International Economic Studies, University of Stockholm, Seminar Paper No. 588.
- Gutiérrez, E. (1994), "Un modelo de devaluaciones para el SME", CEMFI, Documento de Trabajo 9416.
- Hansen, B. E (1992): "Testing for parameter instability in linear models". Journal of Policy Modelling, 14.
- Harvey, A.C (1990), The Econometric Analysis of Time Series, 2nd edn. Hemel Hempstead: Phillip Allan.

- Krugman, P. (1991), "Target Zones and Exchange Rate Dynamics", Quarterly Journal of Economics, 106.
- MacDonald, R. and M.P. Taylor (1989), "Economic Analysis of Foreign Exchange Markets: An Expository Survey", in R. MacDonald and M.P. Taylor, eds., Exchange Rate and Open Economy Macroeconomics, Oxford, UK, and Cambridge, MA, Basil Blackwell.
- McFadden. D.L. (1984), "Econometric Analysis of Qualitative Response Models", in Z. Griliches and M.D. Intrilligator, eds., Handbook of Econometrics, vol. II, Amsterdam, North-Holland.
- Meese, R.A. and K. Rogoff (1983), "The Out-of-Sample Failure of Empirical Exchange Rate Models", in J. Frenkel, ed. Exchange Rates and International Macroeconomics, Chicago, University of Chicago Press.
- Mizrach, B. (1993), "Target Zone Models with Stochastic Realignments: An Econometric Evaluation", Federal Reserve Bank of New York, Working Paper 93-02.
- Pérez-Jurado, M. and J.L. Vega (1993), "Paridad del poder de compra: un análisis empírico", Investigaciones Económicas, vol 18, No. 3. There is an English version in Banco de España Working Paper 9322.
- Ramsey, J.B (1969), "Tests for specification errors in classical linear least square regression analysis", Journal of The Royal Statistical Society, 31.
- Vlaar, P. (1994), "Exchange Rates and Risk Premia within the EMS". Thesis. Maastricht University.
- White, H. (1980), "A heteroskedastic-consistent covariance matrix estimator and a direct test for heteroskedasticity". Econometrica, 48.

WORKING PAPERS (1)

- 9429 **Susana Núñez:** Perspectivas de los sistemas de pagos: una reflexión crítica.
- 9430 **José Viñals:** ¿Es posible la convergencia en España?: En busca del tiempo perdido.
- 9501 **Jorge Blázquez y Miguel Sebastián:** Capital público y restricción presupuestaria gubernamental.
- 9502 **Ana Buisán:** Principales determinantes de los ingresos por turismo.
- 9503 **Ana Buisán y Esther Gordo:** La protección nominal como factor determinante de las importaciones de bienes.
- 9504 **Ricardo Mestre:** A macroeconomic evaluation of the Spanish monetary policy transmission mechanism.
- 9505 **Fernando Restoy and Ana Revenga:** Optimal exchange rate flexibility in an economy with intersectoral rigidities and nontraded goods.
- 9506 **Ángel Estrada and Javier Vallés:** Investment and financial costs: Spanish evidence with panel data. (The Spanish original of this publication has the same number.)
- 9507 **Francisco Alonso:** La modelización de la volatilidad del mercado bursátil español.
- 9508 **Francisco Alonso y Fernando Restoy:** La remuneración de la volatilidad en el mercado español de renta variable.
- 9509 **Fernando C. Ballabriga, Miguel Sebastián y Javier Vallés:** España en Europa: asimetrías reales y nominales.
- 9510 **Juan Carlos Casado, Juan Alberto Campoy y Carlos Chuliá:** La regulación financiera española desde la adhesión a la Unión Europea.
- 9511 **Juan Luis Díaz del Hoyo y A. Javier Prado Dominguez:** Los FRAs como guías de las expectativas del mercado sobre tipos de interés.
- 9512 **José M.ª Sánchez Sáez y Teresa Sastre de Miguel:** ¿Es el tamaño un factor explicativo de las diferencias entre entidades bancarias?
- 9513 **Juan Ayuso y Soledad Núñez:** ¿Desestabilizan los activos derivados el mercado al contado?: La experiencia española en el mercado de deuda pública.
- 9514 **M.ª Cruz Manzano Frías y M.ª Teresa Sastre de Miguel:** Factores relevantes en la determinación del margen de explotación de bancos y cajas de ahorros.
- 9515 **Fernando Restoy and Philippe Weil:** Approximate equilibrium asset prices.
- 9516 **Gabriel Quirós:** El mercado francés de deuda pública.
- 9517 **Ana L. Revenga and Samuel Bentolila:** What affects the employment rate intensity of growth?
- 9518 **Ignacio Iglesias Araúzo y Jaime Esteban Velasco:** Repos y operaciones simultáneas: estudio de la normativa.
- 9519 **Ignacio Fuentes:** Las instituciones bancarias españolas y el Mercado Único.
- 9520 **Ignacio Hernando:** Política monetaria y estructura financiera de las empresas.
- 9521 **Luis Julián Álvarez y Miguel Sebastián:** La inflación latente en España: una perspectiva macroeconómica.
- 9522 **Soledad Núñez Ramos:** Estimación de la estructura temporal de los tipos de interés en España: elección entre métodos alternativos.
- 9523 **Isabel Argimón, José M. González-Páramo y José M.ª Roldán Alegre:** Does public spending crowd out private investment? Evidence from a panel of 14 OECD countries.

- 9524 **Luis Julián Álvarez, Fernando C. Ballbriga y Javier Jareño:** Un modelo macroeconómico trimestral para la economía española.
- 9525 **Aurora Alejano y Juan M.ª Peñalosa:** La integración financiera de la economía española: efectos sobre los mercados financieros y la política monetaria.
- 9526 **Ramón Gómez Salvador y Juan J. Dolado:** Creación y destrucción de empleo en España: un análisis descriptivo con datos de la CBBE.
- 9527 **Santiago Fernández de Lis y Javier Santillán:** Regímenes cambiarios e integración monetaria en Europa.
- 9528 **Gabriel Quirós:** Mercados financieros alemanes.
- 9529 **Juan Ayuso Huertas:** Is there a trade-off between exchange rate risk and interest rate risk? (The Spanish original of this publication has the same number.)
- 9530 **Fernando Restoy:** Determinantes de la curva de rendimientos: hipótesis expectacional y primas de riesgo.
- 9531 **Juan Ayuso and María Pérez Jurado:** Devaluations and depreciation expectations in the EMS.
- 9532 **Paul Schulstad and Ángel Serrat:** An Empirical Examination of a Multilateral Target Zone Model.
- 9601 **Juan Ayuso, Soledad Núñez and María Pérez-Jurado:** Volatility in Spanish financial markets: The recent experience.
- 9602 **Javier Andrés e Ignacio Hernando:** ¿Cómo afecta la inflación al crecimiento económico? Evidencia para los países de la OCDE.
- 9603 **Barbara Dluhosch:** On the fate of newcomers in the European Union: Lessons from the Spanish experience.
- 9604 **Santiago Fernández de Lis:** Classifications of Central Banks by Autonomy: A comparative analysis.
- 9605 **M.ª Cruz Manzano Frías y Sofía Galmés Belmonte:** Políticas de precios de las entidades de crédito y tipo de clientela: efectos sobre el mecanismo de transmisión.
- 9606 **Malte Krüger:** Speculation, Hedging and Intermediation in the Foreign Exchange Market.
- 9607 **Agustín Maravall:** Short-Term Analysis of Macroeconomic Time Series.
- 9608 **Agustín Maravall and Christophe Planas:** Estimation Error and the Specification of Unobserved Component Models.
- 9609 **Agustín Maravall:** Unobserved Components in Economic Time Series.
- 9610 **Matthew B. Canzoneri, Behzad Diba and Gwen Eudey:** Trends in European Productivity and Real Exchange Rates.
- 9611 **Francisco Alonso, Jorge Martínez Pagés y María Pérez Jurado:** Agregados monetarios ponderados: una aproximación empírica.
- 9612 **Agustín Maravall and Daniel Peña:** Missing Observations and Additive Outliers in Time Series Models.
- 9613 **Juan Ayuso and Juan L. Vega:** An empirical analysis of the peseta's exchange rate dynamics.

(1) Previously published Working Papers are listed in the Banco de España publications catalogue.

<p>Queries should be addressed to: Banco de España Sección de Publicaciones. Negociado de Distribución y Gestión Telephone: 338 51 80 Alcalá, 50. 28014 Madrid</p>
--